## Multiple blowing-up solutions for the singular Liouville equation on closed surfaces

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## Abstract

Let  $(\Sigma, g)$  be a compact surface without boundary endowed with metric g. We are concerned with the existence of blowing-up solutions when the parameter  $\rho$  approaches the critical values  $8\pi\mathbb{N}$  for the following singular Liouville equation:

$$-\Delta_g u = \rho \left( \frac{h(x)e^u}{\int_{\Sigma} h(x)e^u \, dV_g} - \frac{1}{|\Sigma|} \right) - 4\pi \sum_{i=1}^{\ell} \alpha_i \left( \delta_{p_i} - \frac{1}{|\Sigma|} \right),$$

where  $\rho > 0$ ,  $h : \Sigma \to \mathbb{R}$  is a smooth positive function, the points  $p_i \in \Sigma$  are the singular sources with weights  $\alpha_i > 0$ . Here  $\delta_p$  denotes the Dirac mass measure supported at p and  $|\Sigma|$  is the area of  $\Sigma$ .

In particular, by employing a min-max scheme jointly with a finite dimensional reduction method, we construct solutions exhibiting a *blow-up* behavior near a finitely many number of points of  $\Sigma$ . We then discuss how new existence results may be deduced in a perturbative regime for the case of the sphere.

This is joint work with P. Esposito (Rome Tre University).

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